The active oxygen complexes formed upon reaction of ferric hemoproteins of ferriporphyrins with single oxygen donors such as iodosylarenes have been described as  $Fe^{V}=0$ ,  ${}^{8b,15,20}$ ,  $Fe^{IV}=0$ (porphyrin  $\pi$  cation radical),  ${}^{3,4,15}$  or  $Fe^{IV}R$ . (R being an amino acid residue)  ${}^{3b,18}$  complexes. In some cases, the occurrence of structure B which involves the iron in a peculiar coordination environment but in its usual ferric state should also be considered.<sup>21</sup>

(19) Involving the electrophilic reaction of the oxygen atom of CAT I driven by the regeneration of the Fe–N bond, which can be schematically

$$N \rightarrow Fe^{\frac{m}{2}} O N + H \rightarrow X \rightarrow O \rightarrow H \rightarrow N \rightarrow Fe^{\frac{m}{2}} O H$$

$$N \rightarrow Fe^{\frac{m}{2}} O H$$

$$N \rightarrow Fe^{\frac{m}{2}} N + H_{2}O + X = O$$

viewed as

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## Site Symmetry and the Framework Group

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In a recent article in this journal, Pople proposed the useful concept of a *framework group*<sup>1</sup> in order to specify molecular symmetry more completely than is accomplished by using only point group notation. This formalism appears especially useful for machine computations of structures from the symmetry notation and vice versa. The purpose of this communication is to recast the formalism in terms of site symmetry groups.<sup>2</sup> There are several advantages to this: (a) The subsets of atoms can be easily shown to be mutually exclusive, since the site symmetry and interchange groups share no common generators.<sup>2b</sup> (b) Pople's k values are simply the order of the interchange groups, which, in turn, are the orders of the full point groups divided by those of the site symmetry groups. (c) The site symmetry terminology is already in the literature, thus avoiding the introduction of the new terminology (the O, X, etc., labels). (d) Most importantly, computational advantages are obtained in the construction of linear combinations of basis functions. These are obtained by the successive application of the site symmetry and interchange group projection operators.2b

The site symmetry group,  $G_s$ , of a site in a molecule is the group defined by the symmetry elements which pass through that site. The interchange group,  $G_I$ , is the group which interchanges the equivalent sites and is defined by the generators of the full group which are not included in the site symmetry.<sup>2b</sup> Table I lists the site symmetry and interchange groups for some selected systems. Both the site symmetry and the interchange groups for a position can be as high as the full point symmetry or as low as  $C_1$ . The generators of the point group appear in one or the other of these, but they cannot appear in both. Thus, subsets of atoms having

Table I. Site Symmetry and Interchange Groups for Some Selected Systems<sup>3</sup>

point group	moleculea	ligand	G <sub>s</sub>	$G_I$
C_3v	AX <sub>3</sub>	x	$C_s$	<i>C</i> <sub>3</sub>
	AX <sub>3</sub> Y	Y	$C_{3v}$	$C_1$
$C_{4n}$	AX.	Х	$C_s$	$C_{4}$
	AX₄YZ	Y(Z)	$\tilde{C}_{AD}$	$C_1$
$C_{nn}$	$AX_n$	X	$C_s^{\sim}$	$C_n^{\cdot}$
$D_{2h}$	AX, Y, Z,	X(Y,Z)	$\tilde{C}_{n}$	$C_{2}$
$D_{2d}$	AX,Y,	X(Y)	$C_{s}^{r}$	D,
$D_{3h}$	AX,	X	$C_{2n}$	$C_{3}$
	AX, Y,	Y	$C_{3v}$	С,
$D_{3d}$	AX <sub>6</sub>	Х	$C_s^{s}$	$S_6$
$D_{4h}$	AX <sub>4</sub>	Х	$\tilde{C}_{,n}$	Č₄
	AX <sub>4</sub> Y,	Y	$C_{4\nu}^{2\nu}$	С,
$D_{6h}$	X <sub>6</sub>	Х	$C_{,v}$	$C_6^{-}$
$T_d$	AX₄	Х	$C_{3v}$	$S_{4}$
$\tilde{O_h}$	AX <sub>6</sub>	Х	$C_{4v}$	$S_4$
$D_{\infty h}$	X <sub>2</sub>	х	$C_{\infty v}^{n}$	$C_i$

<sup>a</sup> The A atom in each case has the full point symmetry as its site symmetry and  $C_1$  as its interchange symmetry.

Table II. Site Symmetries and k Values

group	site symmetries	k values	
$\overline{C_1}$	C <sub>1</sub>	1	
$C_s$	$C_s, C_1$	1, 2	
$C_i$	$C_i, C_i$	1, 2	
$C_n$	$C_n, C_1$	1, <i>n</i>	
<i>C</i> ,,,	$C_{11}$ , $C_{s}$ , $C_{s}$ , $C_{s}$	1, 2, 2, 4	
$C_{nv}$ (n odd)	$C_{nin}$ $C_{s}$ $C_{i}$	1, n, 2n	
$C_{nn}$ ( <i>n</i> even)	$C_{nun} C_{\alpha} C_{\alpha}^{\prime}, C_{\alpha}$	1, n, n, 2n	
Cnh	Cnn Cn Ca C	1, 2, n, 2n	
S <sub>n</sub>	$S_{1n}, C_n, C_n$	1, 2, 2n	
$D_n$ (n odd)	$D_n, C_n, C_n, C_n$	1, 2, n, 2n	
$D_n$ (n even)	$D_{n}, C_{n}, C_{n}, C_{n}, C_{n}, C_{n}$	1, 2, n, n, 2n	
$D_{nd}$	$D_{nd}$ , $C_{nv}$ , $C_{n}$ , $C_{n}$ , $C_{n}$	1, 2, 2n, 2n, 4n	
D.h	$D_{\rm ch}$ , $C_{\rm cur}$ , $C_{\rm cur}$ , $C_{\rm cur}$ , $C_{\rm cur}$	1, 2, 2, 2, 4, 4, 4, 8	
- 211	$C_{0}^{\prime}, C_{0}^{\prime}, C_{1}^{\prime}$	-, -, -, -, -, -, -, -, -, -, -	
$D_{nh}$ (n odd)	Dub, Cum Can Ca Ca, C	1, 2, n, 2n, 2n, 4n	
$D_{nh}$ ( <i>n</i> even)	$D_{nh}$ $C_{nin}$ $C_{ain}$ $C_{ain}$ $C_{ain}$	1, 2, n, n, 2n, 2n, 2n, 4n	
- 111 ( )	$C_{0}^{*}, C_{0}^{*}, C_{1}^{*}$	_,_,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	
Т	T. C. C. C. C.	1, 4, 6, 12	
$\overline{T}_{d}$	$T_{d}$ , $C_{ave}$ , $C_{ave}$ , $C_{a}$ , $C_{e}$	1, 4, 6, 12, 24	
$T_{\rm h}$	$T_{\rm h}, C_{\rm s}, C_{\rm s}, C_{\rm s}, C_{\rm s}$	1. 8. 6. 12. 24	
O	O, C, C, C, C, C, C	1, 6, 8, 12, 24	
0 <sub>h</sub>	$O_{h}$ $C_{uh}$ $C_{ah}$ $C_{ah}$ $C_{ah}$ $C_{ah}$	1, 6, 8, 12, 24, 24, 48	
- 11	$C_{2}$ , $C_{1}$	-, -, -, -, -, -, -, -, -, -,	
Ι	I, C, C, C, C, C	1, 12, 20, 30, 60	
In	$I_{h}, C_{ih}, C_{ah}, C_{ah}, C_{ah}, C_{ah}, C_{ah}$	1, 12, 20, 30, 60, 120	
С.,,,	$C_{\text{out}} = C_{\text{o}}$	1. ∞	
Dh	$D_{ab}$ , $C_{ab}$ , $C_{ab}$ , $C_{ab}$	1, 2, ∞, ∞	
~/•	with with 70% = 3	· · · ·	

Table III. Correlation of  $C_{3v}$  and  $S_4$  with  $T_d$ 



different site symmetries are mutually exclusive.

Recasting the framework group in terms of the site symmetry groups amounts to using the site symmetry labels instead of the  $O, C_n, X$ , etc., labeling used by Pople. The O label is always replaced by the label of the point group, and the X label always by  $C_1$ . The other labels depend upon which symmetry elements pass through the points. Table II presents Table I of ref 1 in the new notation. The framework notation for a particular molecule can be derived by the obvious substitutions. For example, a tetrahedral XY<sub>4</sub> molecule would be classified  $T_d(T_d(X), 4C_{3e}(Y))$ 

<sup>(1)</sup> J. A. Pople, J. Am. Chem. Soc., 102, 4615 (1980).

 <sup>(2) (</sup>a) R. L. Flurry, Jr., Int. J. Quantum Chem., S6, 455 (1972); (b)
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 "Symmetry Groups: Theory and Chemical Applications", Prentice-Hall, Englewood Cliffs, NJ, 1980.

<sup>(3)</sup> Reference 2d, p 218.

(the notation  $T_d[T_d(X), C_{3v}(Y)]$  is actually sufficient). The notation for CH<sub>2</sub>F<sub>2</sub> would be  $C_{2\nu}[C_{2\nu}(C), C_s(H), C_s'(F)]$ . That for the porphine diamion (1) would be  $D_{4h}[C_{2\nu}(N), C_{2\nu}'(C(1)H), C_{s}]$ . (C(2), C(3)H)]. Tables II-V of ref 1 have their original meaning with the obvious substitution of the new definitions.



For an illustration of the computational utility of site symmetry and interchange groups, consider the construction of symmetry adapted functions from an s and p basis set on each atom of the tetrahedral  $XY_4$  system (2). Let the reference Cartesian axes



be parallel to the  $C_2$  axes. Call the basis functions  $s_i$ ,  $x_i$ ,  $y_i$ , and  $z_i$ . The orientation of the  $x_i$  on the Y atoms should be such that they are interchanged by the operations of the interchange symmetry group and similarly for the  $y_i$  and  $z_i$ . The site symmetry of X is the full  $T_d$  and that for  $Y_i$  is  $C_{30}$ . The respective interchange groups are  $C_1$  and  $S_4$ . A correlation diagram<sup>4</sup> of  $C_{3\nu}$  and  $S_4$  with  $T_d$  is useful. This is given in Table III. This tells us that, for example, a function transforming as the  $A_1$  representation in the  $C_{3v}$  site symmetry and as E under the interchange spans the  $T_2$  representation of  $T_d$ .

For the X atom,  $s_5$  transforms as  $A_1$  within  $T_d$ , while  $x_5$ ,  $y_5$ , and  $z_5$  together transform as  $T_2$ . For  $Y_1$ ,  $s_1$  transforms as  $A_1$ , while  $x_1, y_1$ , and  $z_1$  span  $A_1 + E$ . By using the projection operators,  $P^{\Gamma}$ , from  $C_{3v}$ , the symmetry adapted combinations of  $x_1, y_1$ , and  $z_1$  are

$$P^{A_1}x_1 = (1/\sqrt{3})(x_1 + y_1 + z_1) \equiv a_1 \tag{1}$$

$$P^{E}x_{1} = (1/\sqrt{6})(2x_{1} - y_{1} - z_{1}) \equiv e_{1}$$
(2)

$$P^{E'}x_1 = (1/\sqrt{2})(y_1 - z_1) \equiv p_1 \tag{3}$$

(where eq 2 and 3 are the two orthogonal components of the Efunction.) The symmetry adapted functions in  $T_d$  can be obtained by applying the appropriate  $S_4$  projection operators to  $s_1$ ,  $a_1$ ,  $e_1$ , and  $p_1$ . We have for the  $A_1$  functions

$$P^{A}s_{1} = N(s_{1} + s_{2} + s_{3} + s_{4}) \equiv \lambda_{1}^{A_{1}}$$
(4)

$$P^{A}a_{1} = N(a_{1} + a_{2} + a_{3} + a_{4}) = N(x_{1} + x_{2} + x_{3} + x_{4} + y_{1} + y_{2} + y_{3} + y_{4} + z_{1} + z_{2} + z_{3} + z_{4}) \equiv \lambda_{2}^{A_{1}} (5)$$

where the N's are normalizing constants. Several combinations are possible for the degenerate E,  $T_1$ , and  $T_2$  functions. Unique combinations should be chosen. The combinations EB for E, EE for  $T_1$ , and  $A_1B$  and EE for  $T_2$ , where the first listed representation is from the site symmetry and the second from the interchange,

are suitable choices. The two components of the E representation of  $S_4$  acting on the same component of the E from  $C_{3n}$  give the  $T_1$  and  $T_2$  functions. We have for one component of the E functions

$$P^{B}e_{1} = N(e_{1} - e_{2} + e_{3} - e_{4}) = N[2(x_{1} - x_{2} + x_{3} - x_{4}) - (y_{1} - y_{2} + y_{3} - y_{4}) - (z_{1} - z_{2} + z_{3} - z_{4})] \equiv \lambda^{E} (6)$$

For one component of the  $T_1$  function

$$P^{E}e_{1} = N(e_{1} - e_{3}) = N[2(x_{1} - x_{3}) - (y_{1} - y_{3}) - (z_{1} - z_{3})] \equiv \lambda^{T_{1}} (7)$$

And for one component of each of the  $T_2$  functions

$$P^{\mathbf{B}}s_1 = N(s_1 - s_2 + s_3 - s_4) \equiv \lambda_1^{T_2}$$
(8)

$$P^{B}a_{1} = N(a_{1} - a_{2} + a_{3} - a_{4}) = N(x_{1} - x_{2} + x_{3} - x_{4} + y_{1} - y_{2} + y_{3} - y_{4} + z_{1} - z_{2} + z_{3} - z_{4}) \equiv \lambda_{2}^{T_{2}}$$
(9)  
$$P^{E}e_{1}N(e_{2} - e_{4}) = N[2(x_{2} - x_{4}) - (y_{2} - y_{4}) - (z_{2} - z_{4})] \equiv \lambda_{2}^{T_{2}}$$

$$P^{E}e_{1}N(e_{2}-e_{4}) = N[2(x_{2}-x_{4})-(y_{2}-y_{4})-(z_{2}-z_{4})] \equiv \lambda_{3}^{T_{2}}$$
(10)

## Radical Anion of 1,1-Difluoroethylene. EPR Evidence for a Perpendicular Geometry

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Fluorine substitution is known to have a profound effect on the geometry and electronic structure of alkyl radicals.<sup>1-3</sup> Also, it has been demonstrated that increasing fluorination of the benzene and pyridine radical anions brings about a  $\pi^{*-\sigma^{*}}$  crossover in the electronic structure of these radicals.<sup>4,5</sup> Since previous work has provided strong evidence that the tetrafluoroethylene radical anion is a  $\sigma^*$  radical,<sup>6</sup> we have sought to generate the 1,1-difluoroethylene radical anion in the solid state and compare the structures of these two radicals. We find that the EPR spectrum of  $CF_2 = CH_2^-$  can be uniquely interpreted in terms of a 90° twisted (perpendicular) molecular geometry, the unpaired electron occupying an orbital which can be designated as  $\sigma^*$  (or  $\pi'^*$ )<sup>7</sup> for the CF<sub>2</sub> group and  $\pi$  for the CH<sub>2</sub> group.

The lower spectrum (c) in Figure 1 obtained from a  $\gamma$ -irradiated solution of  $CF_2 = CH_2$  in methylcyclohexane- $d_{14}$  (MCHD) glass shows a pair of broad anisotropic features positioned just inside the lines of atomic hydrogen. Careful studies at 77 K established that these signals were produced to the exclusion of the narrow singlet from the matrix-trapped electron<sup>8</sup> for 1,1-difluoroethylene solutions in both MCHD and 2-methyltetrahydrofuran<sup>9</sup> glasses, thereby proving that these outer features result from electron capture by the solute. Thus, the features are assigned to the outer lines of a triplet spectrum resulting from hyperfine interaction with the two fluorines<sup>10</sup> in  $CF_2 = CH_2$ , the center line being

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